



**CHEG 3128**

# Battery – 1

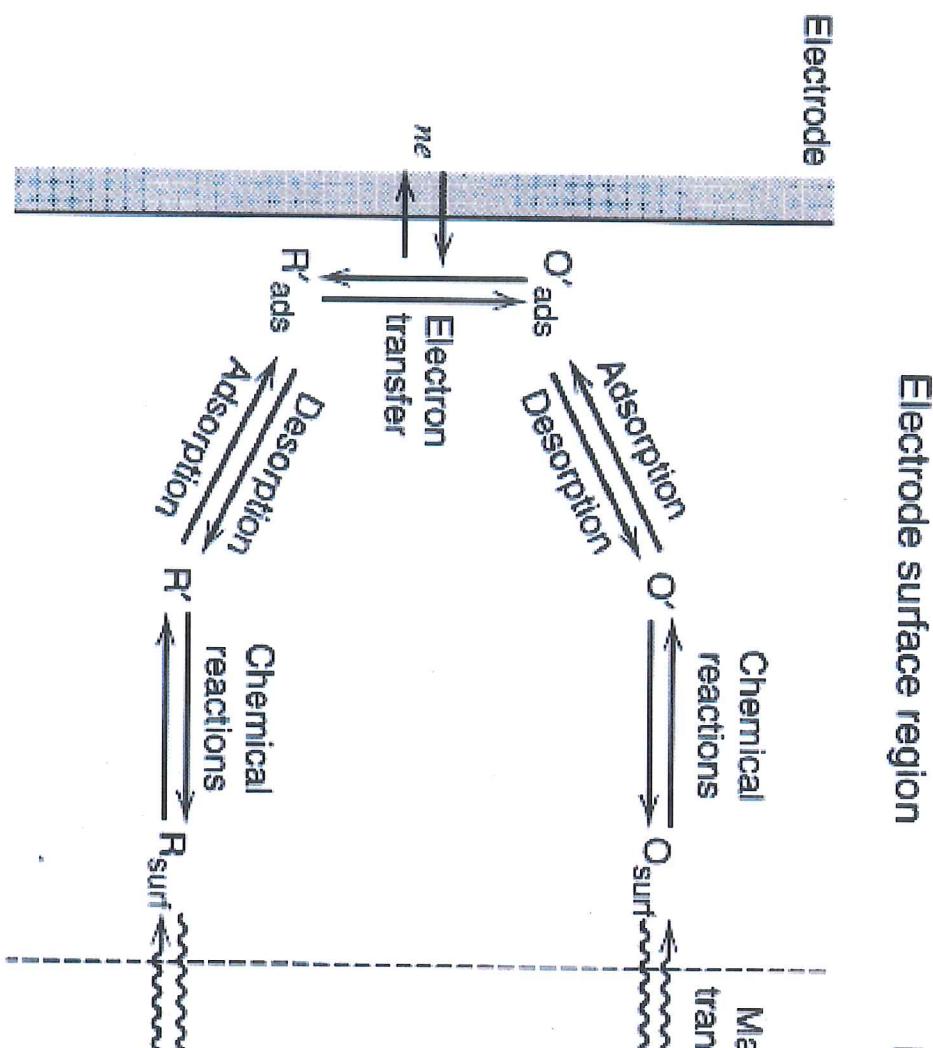
## Electrochemical Fundamentals

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# Redox Processes

- Reduction
- Electron Accepting
  - $O + ne^- \rightarrow R$
  - $R \rightarrow O + ne^-$
- Oxidation
- Electron Donating
- Equilibrium
  - $O + ne^- \leftrightarrow R$
- Always written in the reduction form

# All Electrochemical Processes Occur on a surface



# Types of Reactions

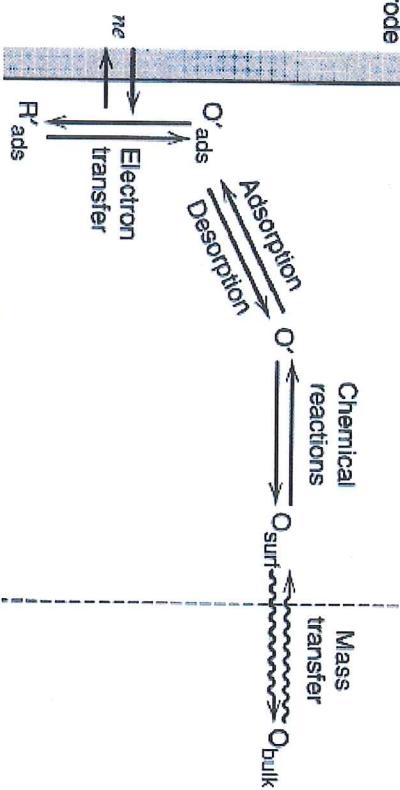
## 1. Electrodeposition (reduction)



Electrode

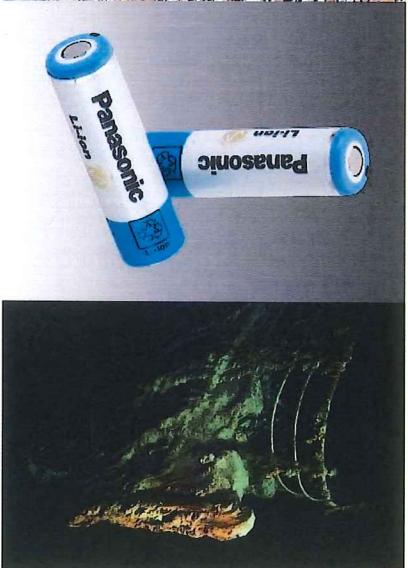
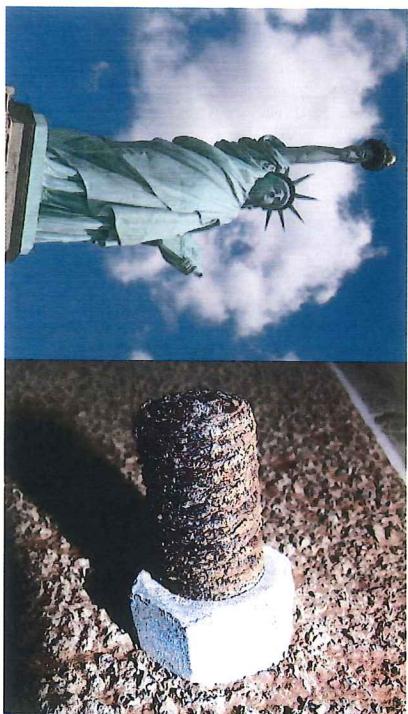
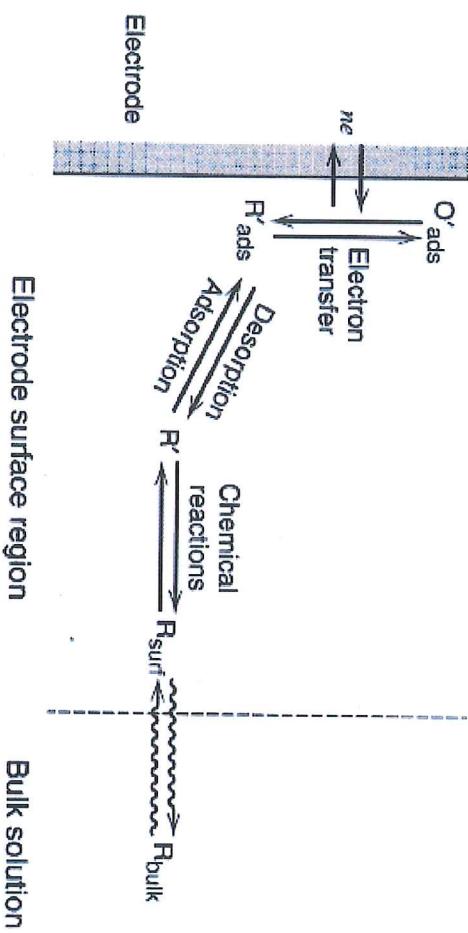
Electrode surface region

Bulk solution



# Types of Reactions

## 2. Corrosion (oxidation)



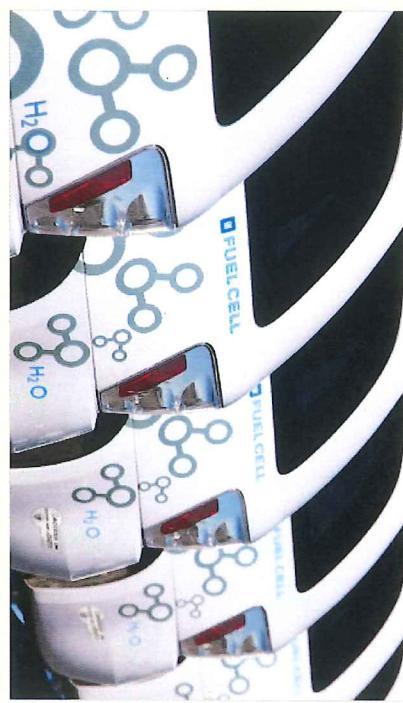
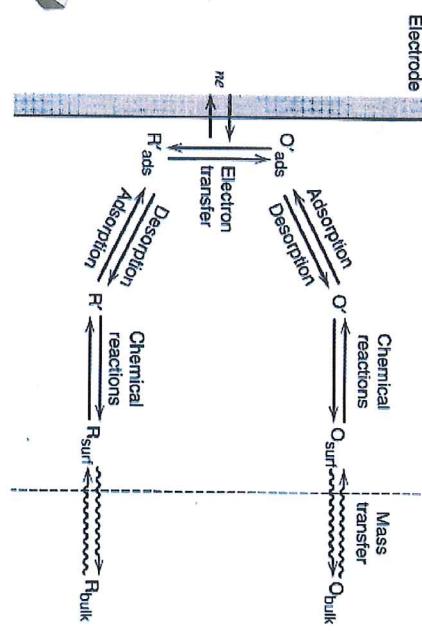
# Types of Reactions

## 3. Electrocatalysis

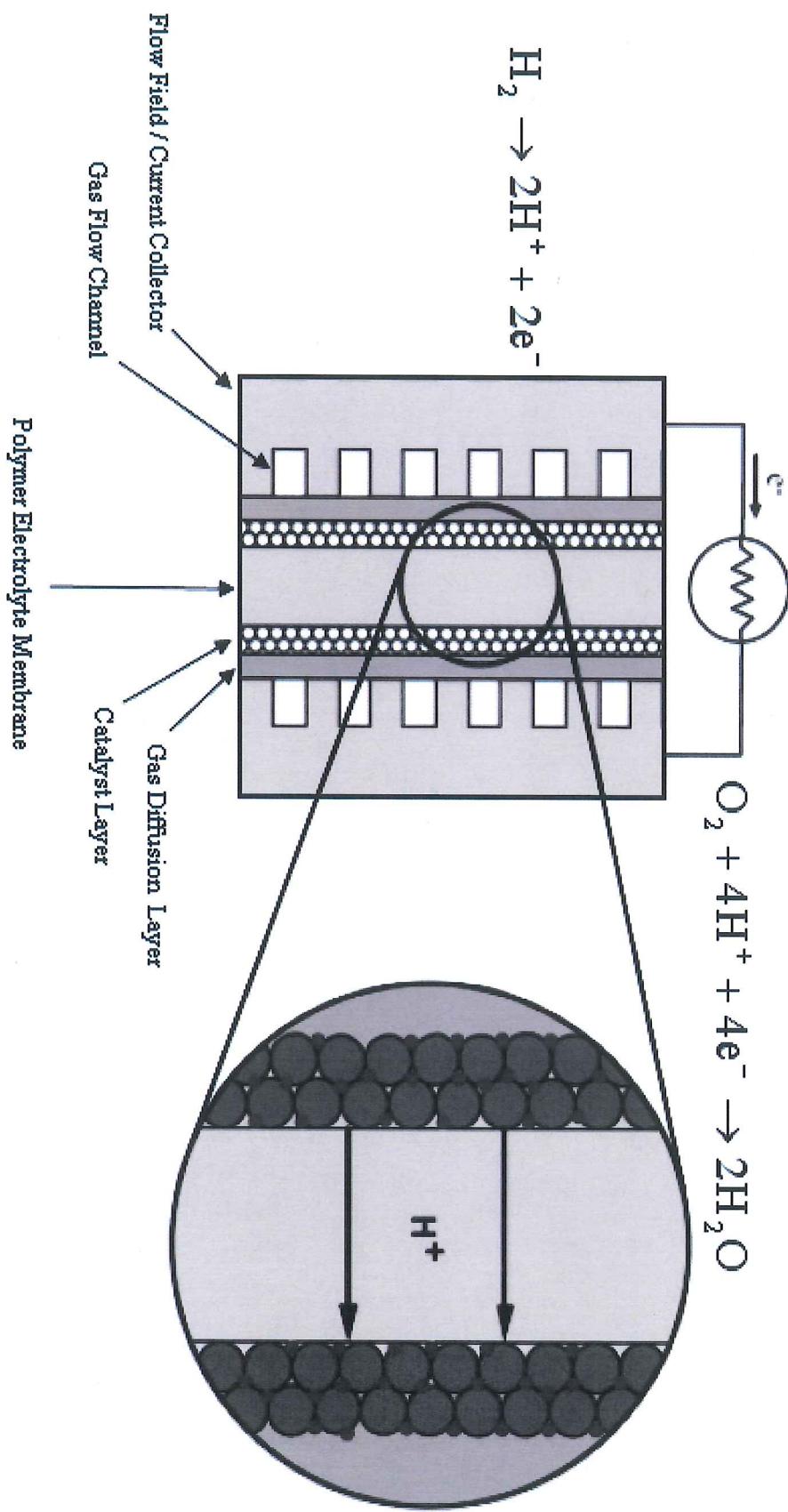
### i) Pure Redox



### ii) Traditional Catalysis



# Example Cell : Proton Exchange Membrane Fuel Cell



# Anode and Cathode

- Faradaic and non-faradaic processes
- Faradaic – electrochemical reactions
  - Note: Electrochemical reactions have both chemical and electrochemical steps! What are the implications?
- Non-faradaic – adsorption/desorption, double layer charging/discharging (we'll discuss this in detail next time)
- Must be electrically conducting
- Minimize distance between them
  - Ionic movement through electrolyte is akin to a pure Ohmic resistance

# Electrolyte

- Liquids: Dissolved salts in a solvent
  - Mostly discuss aqueous in this class
- Solids: Ion conducting groups
- Provides a media for ion transport
- Since the electrolyte solvates the ions (which complete the electrochemical circuit), the reactant must also be solvated in the electrolyte to react
- This leads to the so-called electrochemical “Three Phase Boundary”

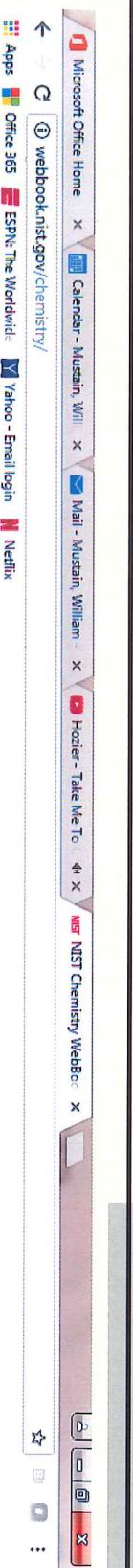
## Three Phase boundary

- For an electrochemical reaction to occur, we MUST have three things present
  - Reactant
  - Catalyst/Electrode
  - Electrolyte
- Designing this interface is critical for device performance
- Void Space
  - Reactant mass transport
- Maximize interface between catalyst and electrolyte



# Chemical Engineering Junior Lab (CHEG 3128) Spring 2017

# NIST Chemistry Webbook



## NIST Chemistry WebBook

### NIST Standard Reference Database Number 69

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#### Search Options top

##### General Searches

- Formula
- Ion energetics properties
- Name
- Vibrational and electronic energies
- IUPAC identifier
- Molecular weight
- CAS registry number
- Reaction
- Author
- Structure

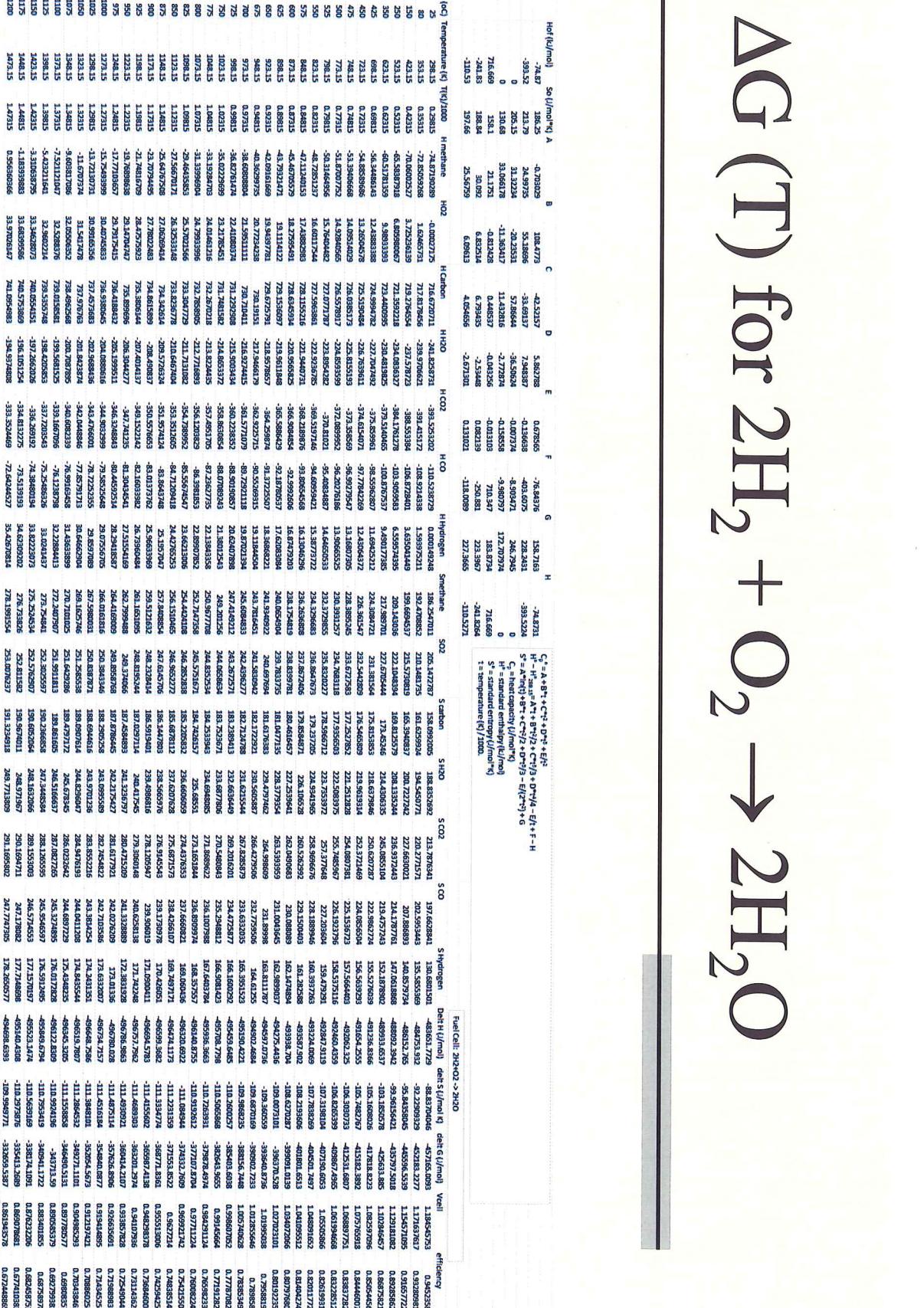
##### Physical Property Based Searches

- Thermophysical Properties of Fluid Systems: High accuracy data for a select group of fluids.
- Group Additivity-Based Estimates: Estimates of gas phase thermodynamic properties based on a submitted structure.
- Formula Brower: Locates chemical species by building up a chemical formula in Hill order.

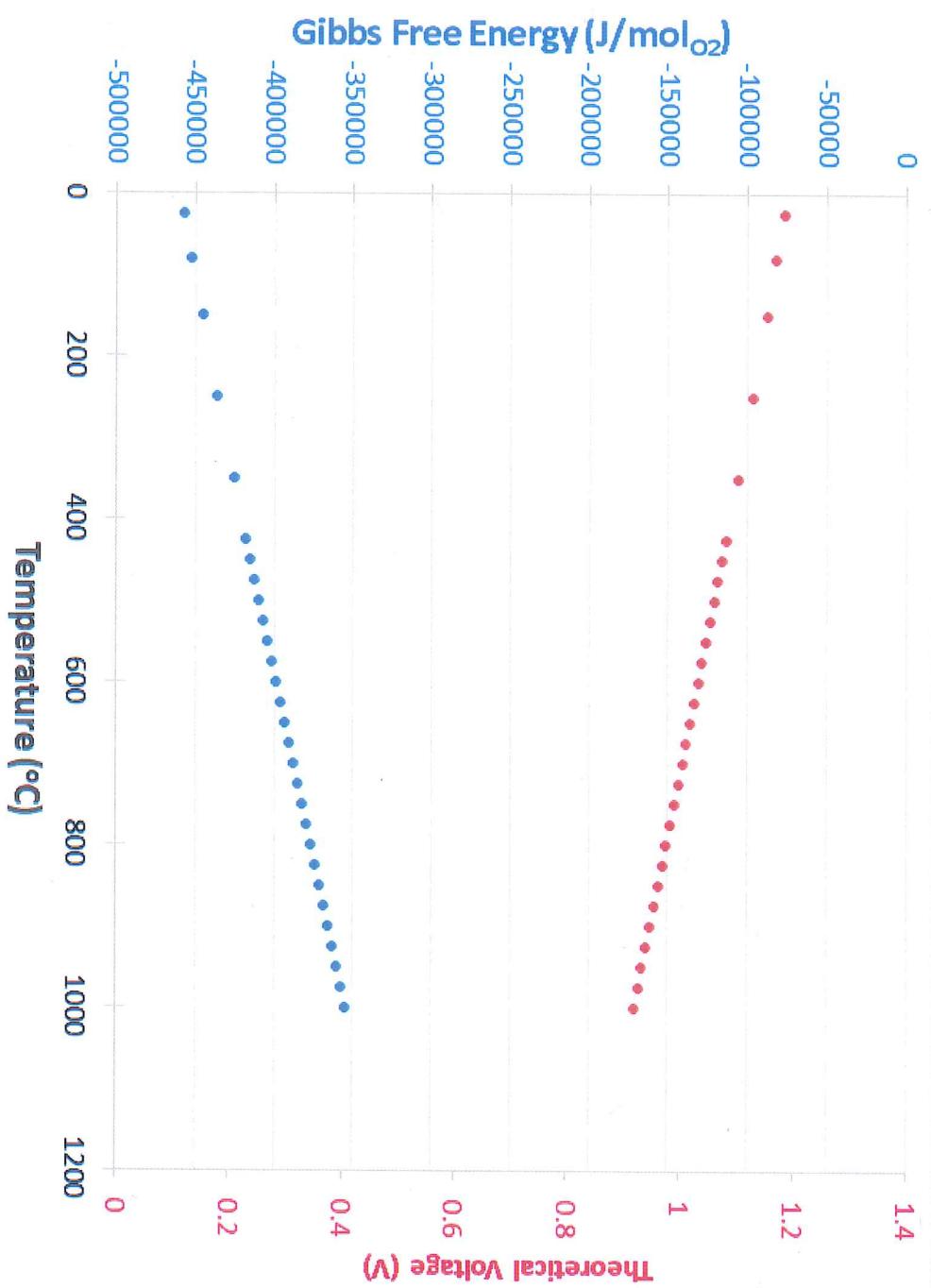
#### Models and Tools top



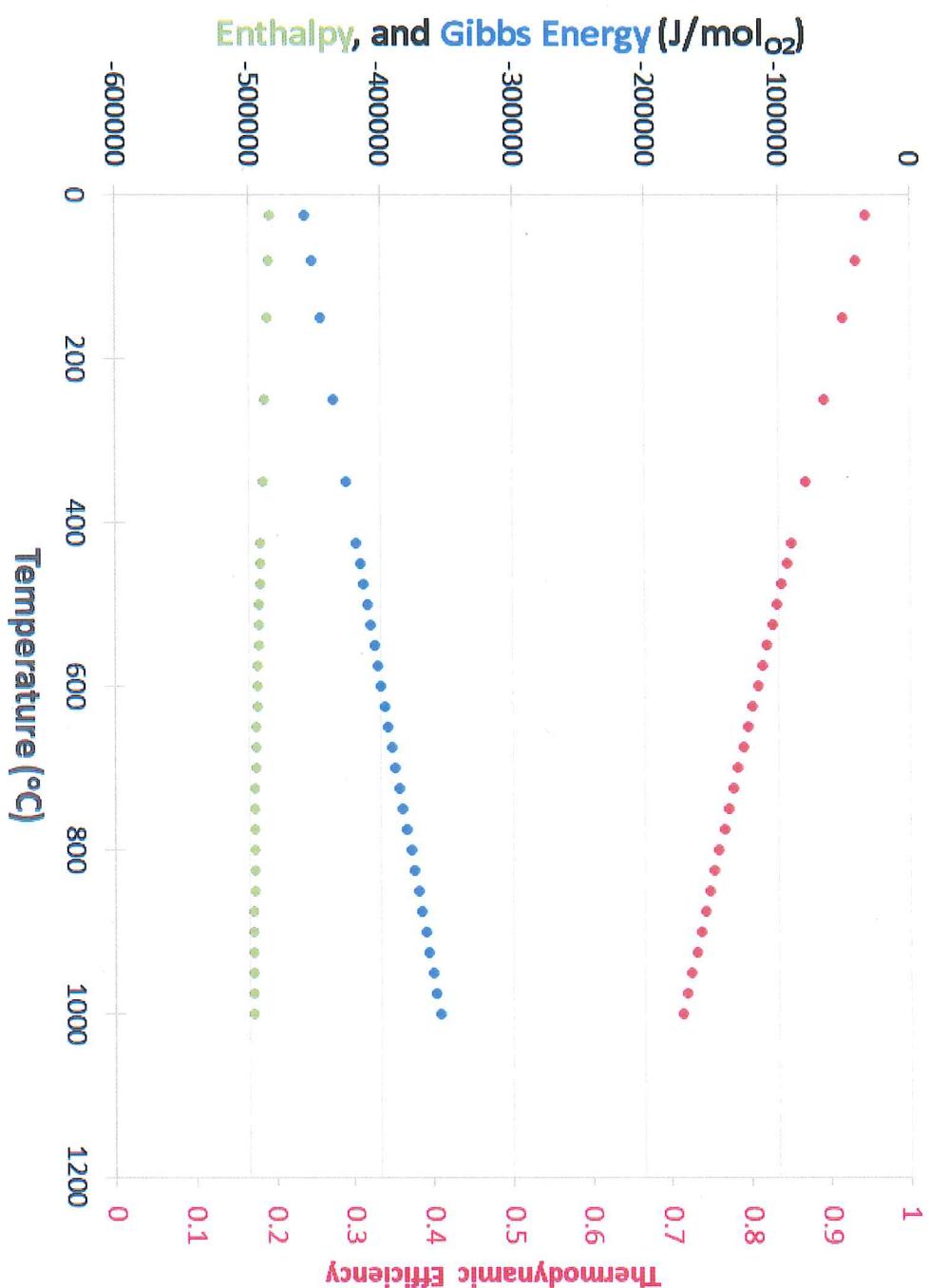
**Chemical Engineering Junior Lab (CHEG 3128)**  
**Spring 2017**



# $\Delta G(T)$ for $2\text{H}_2 + \text{O}_2 \rightarrow 2\text{H}_2\text{O}$



# $\Delta H(T)$ and $\Delta G(T)$ for $2\text{H}_2 + \text{O}_2 \rightarrow 2\text{H}_2\text{O}$



## Extra Resources

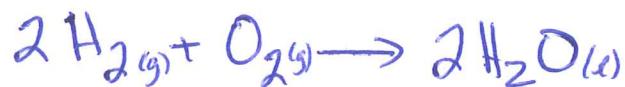
- “Electrochemical Methods: Fundamentals and Applications”, 2<sup>nd</sup> Edition. Allen J. Bard and Larry R. Faulkner.

# CHEG 3128 - Battery 1

All reactions are electron transfer processes

-what I mean is that every reacting system is a combination of complementary redox reactions.

For instance, take the combustion of H<sub>2</sub>



→ Is this spontaneous? Exo/Endo thermic?

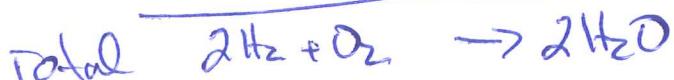
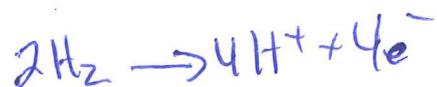
→ How do we capture energy?

→ As heat → ΔH(+)

→ In this reaction, what is oxidized?

" , what is reduced?

What if I write it like this:



Reductions are  $e^-$  accepting reactions

Oxidations are  $e^-$  donatin reactions

$\therefore H$  is oxidized from  $H(0) \rightarrow H(1+)$

$O$  is reduced from  $O(0) \rightarrow O(2-)$

In a chemical system, we recover the energy from this RXN as heat. Hz combustion is used in combined cycle power plants. The combustion heat creates steam, which turns a turbine, spinning a shaft between 2 magnets & looped Cu wire  $\rightarrow$  the rotation of the shaft in the magnetic field (Physics 2!) produces a current.

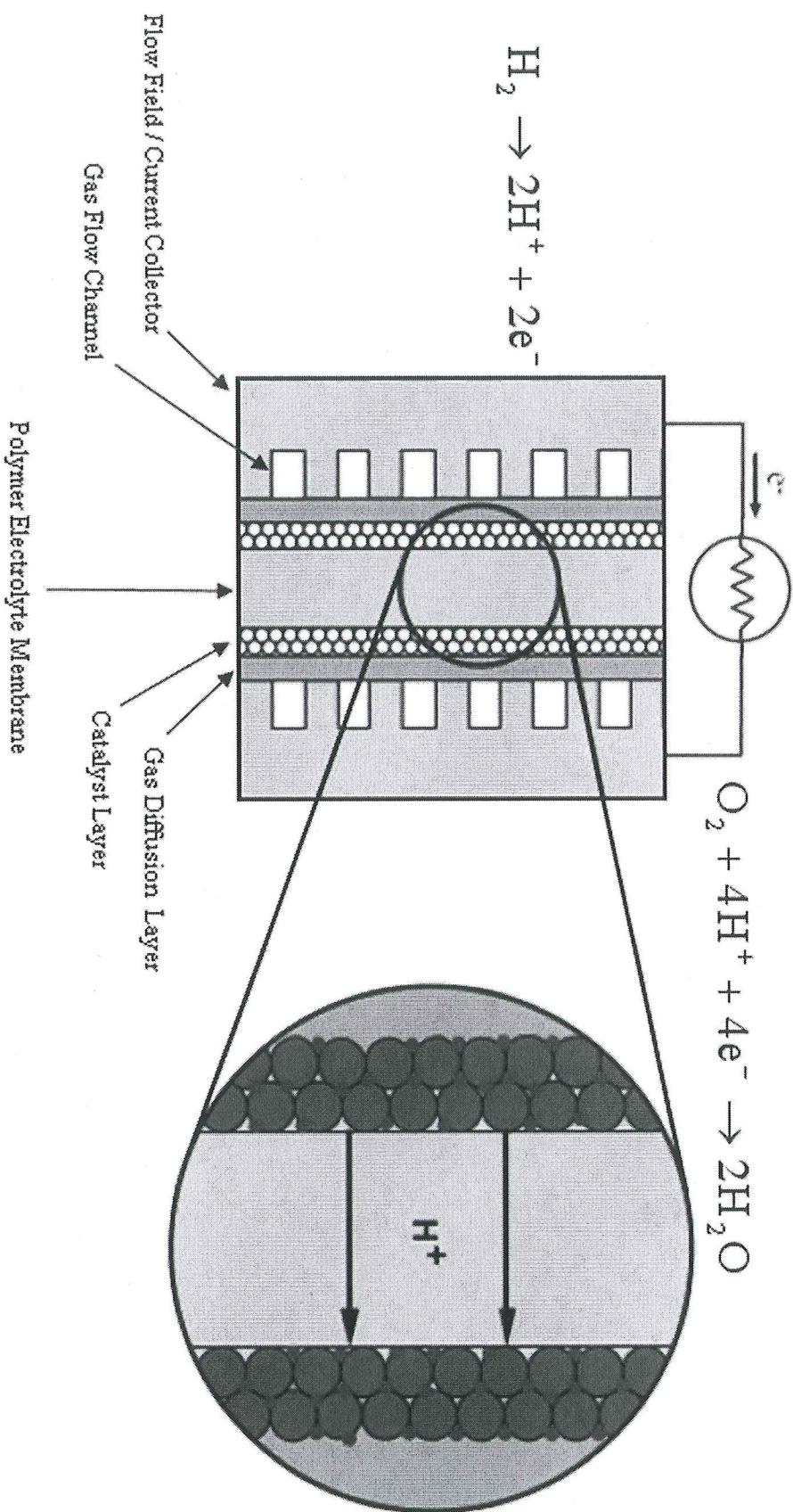
What if we didn't need to do that? What if we could directly use the electrons from the  $1/2$  reactions?  $\rightarrow$  this is electrochemical engineering. One such system is a proton exchange membrane fuel cell.

↳ Diagram on next page

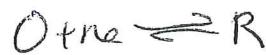
$\rightarrow$  oxidations happen @ the anode  
- (-) "negative" electrode

$\rightarrow$  reduction happen @ the cathode  
- (+) "positive" electrode

How much energy can we get from electrochemical processes?



Let's do an energy / Entropy Balance on one electrode:



### Generalized Energy Balance

$$U_E = U_B + \sum H_{\text{mass}}^{\text{in}} - \sum H_{\text{mass}}^{\text{out}} + Q + W$$

- Break up work term:

$$W = - (P\Delta V + W_{\text{elec}})$$

$$U_E = U_B + \sum H_{\text{mass}}^{\text{in}} - \sum H_{\text{mass}}^{\text{out}} + Q - P\Delta V - W_{\text{elec}}$$

Assumptions: 1) Closed System

2) All electrochemical RXNs are reversible

$$U_E = U_B + Q - P\Delta V - W_{\text{ELEC}}$$

$$S_E = S_B + \frac{Q}{T}$$

$$Q = T\Delta S$$

$$U_E - U_B + P\Delta V = Q - W_{\text{ELEC}}$$

$$\Delta U + P\Delta V = T\Delta S - W_{\text{Elec}}$$

$$\Delta H - T\Delta S = -W_{\text{elec}}$$

$$\Delta G = -W_{\text{elec}}$$

$$W_{\text{elec}} = -\Delta G$$

Units:  $W = \frac{\text{J/mol}}{\text{charge} \cdot \text{potential}} = \frac{\text{ECF}}{\text{charge} \cdot \text{potential}} = Q \cdot E$

$$Q = \frac{\text{charge}}{\text{mole reactant}} = n \cdot F$$

$$\frac{\text{mole e}^-}{\text{mole reactant}} \cdot \frac{\text{C}}{\text{mole e}^-}$$

$$W = -\Delta G = nFE$$

$$\boxed{\Delta G = -nFE}$$



@ STP, 25°C, 1 bar (or 1M)

$$\Delta G^\circ = -nFE^\circ$$

where  $E^\circ$  is called the "Standard Potential"

How to find the standard potential for an individual reaction?

First, Know that we ~~make~~ it impossible to know how much energy ~~we~~ have in a system, which is why we ALWAYS report them as  $\Delta G$ ,  $\Delta H$ , etc.

Therefore, we need an internal standard



$$E^\circ_{H^+/H_2} = 0.0V$$

## Oxygen Reduction in acid media



$$\Delta g_f^\circ, \text{H}_2\text{O} = -237,200 \text{ J/mol}$$

$$\Delta g_f^\circ, \text{O}_2 = 0 \text{ J/mol}$$

$$\Delta g_f^\circ, \text{H}_2 = 0 \text{ J/mol}$$

$$\Delta G^\circ = 2(-237,200 \text{ J/mol}) - [0 \text{ J/mol} + 2(0 \text{ J/mol})]$$

$$\Delta G^\circ = -474,400 \text{ J/mol}$$

$$\Delta G_{\text{RXN}}^\circ = -nFV_{\text{Th}}$$

$$V_{\text{Th}} = \frac{-\Delta G_{\text{RXN}}^\circ}{nF} = \frac{-(-474,400 \text{ J/mol})}{4 \text{ mol/e}^- \cdot 96485.3 \text{ C/mol e}^-} = 1.229 \text{ V}$$

You could also use this to determine specific potentials where reactions occur

$$V_{\text{Th}} = E_{\text{Cathode}}^\circ - E_{\text{Anode}}^\circ$$

↓  
Positive cell voltages mean spontaneous!

↓  
Galvanic cell

$$1.229 = E_{\text{Cathode}}^\circ - 0.0V$$

$$E_{\text{O}_2}^\circ = 1.229 \text{ V}$$

(4)

Do we need to do that work every time?

No → most electrochemical ~~reactions~~ redox couples are tabulated

→ Some can be found in Appendix C

- Page 808 in B&F, Ed 2

→ Also attached to next page

How does our ORR calculated  $E^\circ$  compare with the Table? They are EXACTLY THE SAME!

Now, let's answer our question about the Daniell cell....

What if we attached the Cu foil to the  $\oplus$  terminal

- Cathode



- Zn foil to the  $\ominus$  terminal

- Anode



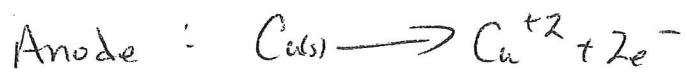
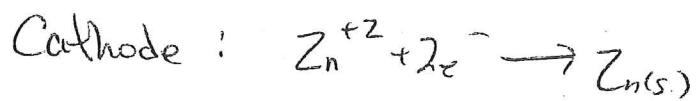
$$E_{\text{Cu/Cu}^{+2}}^{\circ} = 0.34 \text{ V}$$

$$E_{\text{Zn/Zn}^{+2}}^{\circ} = -0.76 \text{ V}$$

$$V_{\text{th}} = E_c^{\circ} - E_A^{\circ} = 0.34 \text{ V} - (-0.76 \text{ V}) = 1.1 \text{ V}$$

$\downarrow$   
galvanic! will occur  
spontaneously

What if we connected this the other way?



$$V_{\text{th}} = E_c^{\circ} - E_A^{\circ} = -0.76 - 0.34 = -1.1 \text{ V}$$

$\downarrow$   
non-spontaneous!  
 $\hookrightarrow$  Electrolytic cell

How would we "recharge" this cell?

Make  $\Delta G < 0$ , so, we have to apply a voltage  $> 1.1 \text{ V}$  on the cell to make it go!

$\rightarrow$  That's why you plug your phone in!

A P P E N D I X

C

REFERENCE TABLES

TABLE C.1 Selected Standard Electrode Potentials  
in Aqueous Solutions at 25°C in V vs. NHE<sup>a</sup>

| Reaction  | Potential, V |
|---|--------------|
| $\text{Ag}^+ + e \rightleftharpoons \text{Ag}$  | 0.7991       |
| $\text{AgBr} + e \rightleftharpoons \text{Ag} + \text{Br}^-$  | 0.0711       |
| $\text{AgCl} + e \rightleftharpoons \text{Ag} + \text{Cl}^-$  | 0.2223       |
| $\text{AgI} + e \rightleftharpoons \text{Ag} + \text{I}^-$  | -0.1522      |
| $\text{Ag}_2\text{O} + \text{H}_2\text{O} + 2e \rightleftharpoons 2\text{Ag} + 2\text{OH}^-$              | 0.342        |
| $\text{Al}^{3+} + 3e \rightleftharpoons \text{Al}$  | -1.676       |
| $\text{Au}^+ + e \rightleftharpoons \text{Au}$  | 1.83         |
| $\text{Au}^{3+} + 2e \rightleftharpoons \text{Au}^+$  | 1.36         |
| $p\text{-benzoquinone} + 2\text{H}^+ + 2e \rightleftharpoons \text{hydroquinone}$                         | 0.6992       |
| $\text{Br}_2(\text{aq}) + 2e \rightleftharpoons 2\text{Br}^-$   | 1.0874       |
| $\text{Ca}^{2+} + 2e \rightleftharpoons \text{Ca}$  | -2.84        |
| $\text{Cd}^{2+} + 2e \rightleftharpoons \text{Cd}$  | -0.4025      |
| $\text{Cd}^{2+} + 2e \rightleftharpoons \text{Cd(Hg)}$  | -0.3515      |
| $\text{Ce}^{4+} + e \rightleftharpoons \text{Ce}^{3+}$  | 1.72         |
| $\text{Cl}_2(\text{g}) + 2e \rightleftharpoons 2\text{Cl}^-$  | 1.3583       |
| $\text{HClO} + \text{H}^+ + e \rightleftharpoons \frac{1}{2}\text{Cl}_2 + \text{H}_2\text{O}$             | 1.630        |
| $\text{Co}^{2+} + 2e \rightleftharpoons \text{Co}$  | -0.277       |
| $\text{Co}^{3+} + e \rightleftharpoons \text{Co}^{2+}$  | 1.92         |
| $\text{Cr}^{2+} + 2e \rightleftharpoons \text{Cr}$  | -0.90        |
| $\text{Cr}^{3+} + e \rightleftharpoons \text{Cr}^{2+}$  | -0.424       |
| $\text{Cr}_2\text{O}_7^{2-} + 14\text{H}^+ + 6e \rightleftharpoons 2\text{Cr}^{3+} + 7\text{H}_2\text{O}$ | 1.36         |
| $\text{Cu}^+ + e \rightleftharpoons \text{Cu}$  | 0.520        |
| $\text{Cu}^{2+} + 2\text{CN}^- + e \rightleftharpoons \text{Cu}(\text{CN})_2^-$                           | 1.12         |
| $\text{Cu}^{2+} + e \rightleftharpoons \text{Cu}^+$   | 0.159        |
| $\text{Cu}^{2+} + 2e \rightleftharpoons \text{Cu}$  | 0.340        |
| $\text{Cu}^{2+} + 2e \rightleftharpoons \text{Cu(Hg)}$  | 0.345        |
| $\text{Eu}^{3+} + e \rightleftharpoons \text{Eu}^{2+}$  | -0.35        |
| $\frac{1}{2}\text{F}_2 + \text{H}^+ + e \rightleftharpoons \text{HF}$                                     | 3.053        |
| $\text{Fe}^{2+} + 2e \rightleftharpoons \text{Fe}$  | -0.44        |
| $\text{Fe}^{3+} + e \rightleftharpoons \text{Fe}^{2+}$  | 0.771        |
| $\text{Fe}(\text{CN})_6^{3-} + e \rightleftharpoons \text{Fe}(\text{CN})_6^{4-}$                          | 0.3610       |

(continued)

TABLE C.1 (*continued*)

| Reaction  | Potential, V |
|---|--------------|
| $2H^+ + 2e \rightleftharpoons H_2$                                | 0.0000       |
| $2H_2O + 2e \rightleftharpoons H_2 + 2OH^-$                       | -0.828       |
| $H_2O_2 + 2H^+ + 2e \rightleftharpoons 2H_2O$                     | 1.763        |
| $2Hg^{2+} + 2e \rightleftharpoons Hg_2^{2+}$                      | 0.9110       |
| $Hg_2^{2+} + 2e \rightleftharpoons 2Hg$                           | 0.7960       |
| $Hg_2Cl_2 + 2e \rightleftharpoons 2Hg + 2Cl^-$                    | 0.26816      |
| $Hg_2Cl_2 + 2e \rightleftharpoons 2Hg + 2Cl^-$ (sat'd. KCl)       | 0.2415       |
| $HgO + H_2O + 2e \rightleftharpoons Hg + 2OH^-$                   | 0.0977       |
| $Hg_2SO_4 + 2e \rightleftharpoons 2Hg + SO_4^{2-}$                | 0.613        |
| $I_2 + 2e \rightleftharpoons 2I^-$                                | 0.5355       |
| $I_3^- + 2e \rightleftharpoons 3I^-$                              | 0.536        |
| $K^+ + e \rightleftharpoons K$                                    | -2.925       |
| $Li^+ + e \rightleftharpoons Li$                                  | -3.045       |
| $Mg^{2+} + 2e \rightleftharpoons Mg$                              | -2.356       |
| $Mn^{2+} + 2e \rightleftharpoons Mn$                              | -1.18        |
| $Mn^{3+} + e \rightleftharpoons Mn^{2+}$                          | 1.5          |
| $MnO_2 + 4H^+ + 2e \rightleftharpoons Mn^{2+} + 2H_2O$            | 1.23         |
| $MnO_4^- + 8H^+ + 5e \rightleftharpoons Mn^{2+} + 4H_2O$          | 1.51         |
| $Na^+ + e \rightleftharpoons Na$                                  | -2.714       |
| $Ni^{2+} + 2e \rightleftharpoons Ni$                              | -0.257       |
| $Ni(OH)_2 + 2e \rightleftharpoons Ni + 2OH^-$                     | -0.72        |
| $O_2 + 2H^+ + 2e \rightleftharpoons H_2O_2$                       | 0.695        |
| $O_2 + 4H^+ + 4e \rightleftharpoons 2H_2O$                        | 1.229        |
| $O_2 + 2H_2O + 4e \rightleftharpoons 4OH^-$                       | 0.401        |
| $O_3 + 2H^+ + 2e \rightleftharpoons O_2 + H_2O$                   | 2.075        |
| $Pb^{2+} + 2e \rightleftharpoons Pb$                              | -0.1251      |
| $Pb^{2+} + 2e \rightleftharpoons Pb(Hg)$                          | -0.1205      |
| $PbO_2 + 4H^+ + 2e \rightleftharpoons Pb^{2+} + 2H_2O$            | 1.468        |
| $PbO_2 + SO_4^{2-} + 4H^+ + 2e \rightleftharpoons PbSO_4 + 2H_2O$ | 1.698        |
| $PbSO_4 + 2e \rightleftharpoons Pb + SO_4^{2-}$                   | -0.3505      |
| $Pd^{2+} + 2e \rightleftharpoons Pd$                              | 0.915        |
| $Pt^{2+} + 2e \rightleftharpoons Pt$                              | 1.188        |
| $PtCl_4^{2-} + 2e \rightleftharpoons Pt + 4Cl^-$                  | 0.758        |
| $PtCl_6^{2-} + 2e \rightleftharpoons PtCl_4^{2-} + 2Cl^-$         | 0.726        |
| $Ru(NH_3)_6^{3+} + e \rightleftharpoons Ru(NH_3)_6^{2+}$          | 0.10         |
| $S + 2e \rightleftharpoons S^{2-}$                                | -0.447       |
| $Sn^{2+} + 2e \rightleftharpoons Sn$                              | -0.1375      |
| $Sn^{4+} + 2e \rightleftharpoons Sn^{2+}$                         | 0.15         |
| $Tl^+ + e \rightleftharpoons Tl$                                  | -0.3363      |
| $Tl^+ + e \rightleftharpoons Tl(Hg)$                              | -0.3338      |
| $Tl^{3+} + 2e \rightleftharpoons Tl^+$                            | 1.25         |
| $U^{3+} + 3e \rightleftharpoons U$                                | -1.66        |
| $U^{4+} + e \rightleftharpoons U^{3+}$                            | -0.52        |
| $UO_2^+ + 4H^+ + e \rightleftharpoons U^{4+} + 2H_2O$             | 0.273        |
| $UO_2^{2+} + e \rightleftharpoons UO_2^+$                         | 0.163        |

(continued)

TABLE C.1 (*continued*)

| Reaction  | Potential, V |
|---|--------------|
| $V^{2+} + 2e \rightleftharpoons V$                      | -1.13        |
| $V^{3+} + e \rightleftharpoons V^{2+}$                  | -0.255       |
| $VO^{2+} + 2H^+ + e \rightleftharpoons V^{3+} + H_2O$   | 0.337        |
| $VO_2^+ + 2H^+ + e \rightleftharpoons VO^{2+} + H_2O$   | 1.00         |
| $Zn^{2+} + 2e \rightleftharpoons Zn$                    | -0.7626      |
| $ZnO_2^{2-} + 2H_2O + 2e \rightleftharpoons Zn + 4OH^-$ | -1.285       |

<sup>a</sup> The data in this table are mainly taken from A. J. Bard, J. Jordan, and R. Parsons, Eds., "Standard Potentials in Aqueous Solutions," Marcel Dekker, New York, 1985 (prepared under the auspices of the Electrochemistry and Electroanalytical Chemistry Commissions of IUPAC). Other sources of standard potentials and thermodynamic data include: (1) A. J. Bard and H. Lund, Eds., "The Encyclopedia of the Electrochemistry of the Elements," Marcel Dekker, New York, 1973–1986. (2) G. Milazzo and S. Caroli, "Tables of Standard Electrode Potentials," Wiley-Interscience, New York, 1977. The data here are referred to the NHE based on a 1-atm standard state for  $H_2$ . See the footnote in Section 2.1.5 concerning the recent change in standard state.

Table C.2 Selected Formal Potentials in Aqueous Solution at 25°C in V vs. NHE<sup>a</sup>

| Reaction   | Conditions              | Potential, V |
|--|-------------------------|--------------|
| $Cu(II) + e \rightleftharpoons Cu$                   | 1 M $NH_3 + 1 M NH_4^+$ | 0.01         |
|  | 1 M KBr                 | 0.52         |
| $Ce(IV) + e \rightleftharpoons Ce(III)$              | 1 M $HNO_3$             | 1.61         |
|  | 1 M HCl                 | 1.28         |
|  | 1 M $HClO_4$            | 1.70         |
|  | 1 M $H_2SO_4$           | 1.44         |
| $Fe(III) + e \rightleftharpoons Fe(II)$              | 1 M HCl                 | 0.70         |
|  | 10 M HCl                | 0.53         |
|  | 1 M $HClO_4$            | 0.735        |
|  | 1 M $H_2SO_4$           | 0.68         |
| $Fe(CN)_6^{3-} + e \rightleftharpoons Fe(CN)_6^{4-}$ | 2 M $H_3PO_4$           | 0.46         |
|  | 0.1 M HCl               | 0.56         |
|  | 1 M HCl                 | 0.71         |
|  | 1 M $HClO_4$            | 0.72         |
| $Sn(IV) + 2e \rightleftharpoons Sn(II)$              | 1 M HCl                 | 0.14         |

<sup>a</sup> The data in this table are taken mainly from G. Charlot, "Oxidation-Reduction Potentials," Pergamon, London, 1958. Additional values are found in J. J. Lingane, "Electroanalytical Chemistry," Interscience, New York, 1958, and L. Meites, Ed., "Handbook of Analytical Chemistry," McGraw-Hill, New York, 1963.

In class: Cu/Zn demo →

Al/"Cu" demo

↳ What is the rxn that is really happening?

↳ how do we know?



"Scale-up" to "practical" solution → Aluminum can



Cu or other rod

→ What happens when we don't have  $\infty$  resistance + current is allowed to flow?

↳ Is this enough energy/power to run anything?

→ Discuss assignment 1 for Battery lab

→ What if our device is not @ STP?

$$\rightarrow \Delta G = \Delta G(T, P, N) \dots$$

Remember:  $\Delta G = \Delta G(T, P, N)$   
↓  
on [C]

How does impact cell voltage?



2 ways to find  $\Delta G(T)$

↓  
1. Method in SVN (attached)  $\rightarrow \Delta G_p$  method

2. Use [webbook.nist.gov/chemistry](http://webbook.nist.gov/chemistry)  
 $\rightarrow$  NIST chemistry Webbook

to find  $\Delta G_f(T)$   $\rightarrow$  Then do  $\Delta G = \text{Products} - \text{Reactants}$

↓  
This is my preferred method,  
but either will work

↓  
Excel spreadsheet attached

↓  
 $\Delta G_{\text{vst}} + V_{\text{vs.t}}$

$\rightarrow$  Also what is efficiency?

$$-\tau_D = \frac{\Delta G}{\Delta H} \quad \rightarrow \text{total } \eta = \left( \frac{\Delta G}{\Delta H} \right) \left( \frac{V}{V_m} \right)$$

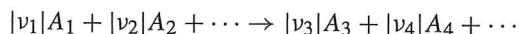
$$\rightarrow \text{Voltage eff} = \frac{V}{V_m}$$

↳ importance?  $\rightarrow$  Later!

## 4.6 TEMPERATURE DEPENDENCE OF $\Delta H^\circ$

In the foregoing sections, standard heats of reaction are discussed for a reference temperature of 298.15 K. In this section we treat the calculation of standard heats of reaction at other temperatures from knowledge of the value at the reference temperature.

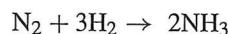
The general chemical reaction may be written:



where  $|v_i|$  is a stoichiometric coefficient and  $A_i$  stands for a chemical formula. The species on the left are reactants; those on the right, products. The sign convention for  $v_i$  is as follows:

*positive (+) for products and negative (-) for reactants*

The  $v_i$  with their accompanying signs are called stoichiometric *numbers*. For example, when the ammonia synthesis reaction is written:



then

$$v_{N_2} = -1 \quad v_{H_2} = -3 \quad v_{NH_3} = 2$$

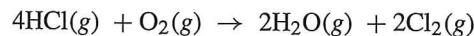
This sign convention allows the definition of a standard heat of reaction to be expressed mathematically by the equation:

$$\Delta H^\circ \equiv \sum_i v_i H_i^\circ \quad (4.14)$$

where  $H_i^\circ$  is the enthalpy of species  $i$  in its standard state and the summation is over all products and reactants. The standard-state enthalpy of a chemical compound is equal to its heat of formation plus the standard-state enthalpies of its constituent elements. If the standard-state enthalpies of all elements are arbitrarily set equal to zero as the basis of calculation, then the standard-state enthalpy of each compound is its heat of formation. In this event,  $H_i^\circ = \Delta H_{f,i}^\circ$  and Eq. (4.14) becomes:

$$\Delta H^\circ = \sum_i v_i \Delta H_{f,i}^\circ \quad (4.15)$$

where the summation is over all products and reactants. This formalizes the procedure described in the preceding section for calculation of standard heats of other reactions from standard heats of formation. Applied to the reaction,



Eq. (4.15) is written:

$$\Delta H^\circ = 2\Delta H_{f,H_2O}^\circ - 4\Delta H_{f,HCl}^\circ$$

With data from Table C.4 for 298.15 K, this becomes:

$$\Delta H_{298}^\circ = (2)(-241,818) - (4)(-92,307) = -114,408 \text{ J}$$

in agreement with the result of Ex. 4.5.

# SVN $\Delta H(T)$

For standard reactions, products and reactants are always at the standard-state pressure of 1 bar. Standard-state enthalpies are therefore functions of temperature only, and by Eq. (2.21),

$$dH_i^\circ = C_{P_i}^\circ dT$$

where subscript  $i$  identifies a particular product or reactant. Multiplying by  $v_i$  and summing over all products and reactants gives:

$$\sum_i v_i dH_i^\circ = \sum_i v_i C_{P_i}^\circ dT$$

Since  $v_i$  is a constant, it may be placed inside the differential:

$$\sum_i d(v_i H_i^\circ) = d \sum_i v_i H_i^\circ = \sum_i v_i C_{P_i}^\circ dT$$

The term  $\sum_i v_i H_i^\circ$  is the standard heat of reaction, defined by Eq. (4.14) as  $\Delta H^\circ$ . The standard heat-capacity change of reaction is defined similarly:

$$\Delta C_P^\circ \equiv \sum_i v_i C_{P_i}^\circ \quad (4.16)$$

As a result of these definitions, the preceding equation becomes:

$d \Delta H^\circ = \Delta C_P^\circ dT$

(4.17)

This is the fundamental equation relating heats of reaction to temperature. Integration gives:

$$\Delta H^\circ = \Delta H_0^\circ + R \int_{T_0}^T \frac{\Delta C_P^\circ}{R} dT \quad (4.18)$$

where  $\Delta H^\circ$  and  $\Delta H_0^\circ$  are heats of reaction at temperature  $T$  and at reference temperature  $T_0$  respectively. If the temperature dependence of the heat capacity of each product and reactant is given by Eq. (4.4), then the integral is given by the analog of Eq. (4.7) ( $\tau \equiv T/T_0$ ):

$$\int_{T_0}^T \frac{\Delta C_P^\circ}{R} dT = (\Delta A)T_0(\tau - 1) + \frac{\Delta B}{2}T_0^2(\tau^2 - 1) + \frac{\Delta C}{3}T_0^3(\tau^3 - 1) + \frac{\Delta D}{T_0} \left( \frac{\tau - 1}{\tau} \right) \quad (4.19)$$

where by definition,

$$\Delta A \equiv \sum_i v_i A_i$$

with analogous definitions for  $\Delta B$ ,  $\Delta C$ , and  $\Delta D$ .

An alternative formulation results when a mean heat capacity change of reaction is defined in analogy to Eq. (4.8):

$$\frac{\langle \Delta C_P^\circ \rangle_H}{R} = \Delta A + \frac{\Delta B}{2}T_0(\tau + 1) + \frac{\Delta C}{3}T_0^2(\tau^2 + \tau + 1) + \frac{\Delta D}{\tau T_0^2} \quad (4.20)$$

Equation (4.18) then becomes:

$$\Delta H^\circ = \Delta H_0^\circ + \langle \Delta C_P^\circ \rangle_H (T - T_0) \quad (4.21)$$

### 13.4 EFFECT OF TEMPERATURE ON THE EQUILIBRIUM CONSTANT

Since the standard-state temperature is that of the equilibrium mixture, the standard property changes of reaction, such as  $\Delta G^\circ$  and  $\Delta H^\circ$ , vary with the equilibrium temperature. The dependence of  $\Delta G^\circ$  on  $T$  is given by Eq. (13.13), which may be rewritten:

$$\frac{d(\Delta G^\circ / RT)}{dT} = \frac{-\Delta H^\circ}{RT^2}$$

In view of Eq. (13.11b), this becomes:

$$\boxed{\frac{d \ln K}{dT} = \frac{\Delta H^\circ}{RT^2}} \quad (13.14)$$

Equation (13.14) gives the effect of temperature on the equilibrium constant, and hence on the equilibrium conversion. If  $\Delta H^\circ$  is negative, i.e., if the reaction is exothermic, the equilibrium constant decreases as the temperature increases. Conversely,  $K$  increases with  $T$  for an endothermic reaction.

If  $\Delta H^\circ$ , the standard enthalpy change (heat) of reaction, is assumed independent of  $T$ , integration of Eq. (13.14) from a particular temperature  $T'$  to an arbitrary temperature  $T$  leads to the simple result:

$$\ln \frac{K}{K'} = -\frac{\Delta H^\circ}{R} \left( \frac{1}{T} - \frac{1}{T'} \right) \quad (13.15)$$

This approximate equation implies that a plot of  $\ln K$  vs. the reciprocal of absolute temperature is a straight line. Figure 13.2, a plot of  $\ln K$  vs.  $1/T$  for a number of common reactions, illustrates this near linearity. Thus, Eq. (13.15) provides a reasonably accurate relation for the interpolation and extrapolation of equilibrium-constant data.

The *rigorous* development of the effect of temperature on the equilibrium constant is based on the definition of the Gibbs energy, written for a chemical species in its standard state:

$$G_i^\circ = H_i^\circ - TS_i^\circ$$

Multiplication by  $v_i$  and summation over all species gives:

$$\sum_i v_i G_i^\circ = \sum_i v_i H_i^\circ - T \sum_i v_i S_i^\circ$$

As a result of the definition of a standard property change of reaction, this reduces to:

$$\Delta G^\circ = \Delta H^\circ - T \Delta S^\circ \quad (13.16)$$

The standard heat of reaction is related to temperature:

$$\Delta H^\circ = \Delta H_0^\circ + R \int_{T_0}^T \frac{\Delta C_P^\circ}{R} dT \quad (4.18)$$

The temperature dependence of the standard entropy change of reaction is developed similarly. Equation (6.21) is written for the standard-state entropy of species  $i$  at the constant standard-state pressure  $P^\circ$ :

$$dS_i^\circ = C_{P,i}^\circ \frac{dT}{T}$$

Multiplying by  $\nu_i$ , summing over all species, and invoking the definition of a standard property change of reaction yields:

$$d\Delta S^\circ = \Delta C_P^\circ \frac{dT}{T}$$

Integration gives:

$$\Delta S^\circ = \Delta S_0^\circ + R \int_{T_0}^T \frac{\Delta C_P^\circ}{R} \frac{dT}{T} \quad (13.17)$$

where  $\Delta S^\circ$  and  $\Delta S_0^\circ$  are standard entropy changes of reaction at temperature  $T$  and at reference temperature  $T_0$  respectively. Equations (13.16), (4.18), and (13.17) are combined to yield:

$$\Delta G^\circ = \Delta H_0^\circ + R \int_{T_0}^T \frac{\Delta C_P^\circ}{R} dT - T \Delta S_0^\circ - RT \int_{T_0}^T \frac{\Delta C_P^\circ}{R} \frac{dT}{T}$$

However,

$$\Delta S_0^\circ = \frac{\Delta H_0^\circ - \Delta G_0^\circ}{T_0}$$

Whence,

$$\Delta G^\circ = \Delta H_0^\circ - \frac{T}{T_0} (\Delta H_0^\circ - \Delta G_0^\circ) + R \int_{T_0}^T \frac{\Delta C_P^\circ}{R} dT - RT \int_{T_0}^T \frac{\Delta C_P^\circ}{R} \frac{dT}{T}$$

Finally, division by  $RT$  yields:

$$\frac{\Delta G^\circ}{RT} = \frac{\Delta G_0^\circ - \Delta H_0^\circ}{RT_0} + \frac{\Delta H_0^\circ}{RT} + \frac{1}{T} \int_{T_0}^T \frac{\Delta C_P^\circ}{R} dT - \int_{T_0}^T \frac{\Delta C_P^\circ}{R} \frac{dT}{T} \quad (13.18)$$

Recall that by Eq. (13.11b),  $\ln K = -\Delta G^\circ/RT$ .

When the temperature dependence of the heat capacity of each species is given by Eq. (4.4), the first integral on the right side of Eq. (13.18) is given by Eq. (4.19), represented for computational purposes by:

$$\int_{T_0}^T \frac{\Delta C_P^\circ}{R} dT = \text{IDCPH}(T_0, T; DA, DB, DC, DD)$$

where "D" denotes " $\Delta$ ". Similarly, the second integral is given by the analog of Eq. (5.15):

$$\int_{T_0}^T \frac{\Delta C_P^\circ}{R} \frac{dT}{T} = \Delta A \ln \tau + \left[ \Delta B T_0 + \left( \Delta C T_0^2 + \frac{\Delta D}{\tau^2 T_0^2} \right) \left( \frac{\tau+1}{2} \right) \right] (\tau-1) \quad (13.19)$$

where

$$\tau \equiv \frac{T}{T_0}$$

Calculating  $\Delta H_{rxn}$  &  $\Delta G_{rxn}$  from  
 Standard Equations  
 ↳ NIST Chemistry Webbook

| Species          | Hof (kJ/mol)    | So (J/mol*K) | A            | B           | C           | D            | E            |
|------------------|-----------------|--------------|--------------|-------------|-------------|--------------|--------------|
| Methane          | -74.87          | 186.25       | -0.703029    | 108.4773    | -42.52157   | 5.862788     | 0.678565     |
| CO2              | -393.52         | 213.79       | 24.99735     | 55.18696    | -33.69137   | 7.948387     | -0.136638    |
| Oxygen           | 0               | 205.15       | 31.32234     | -20.23531   | 57.86644    | -36.50624    | -0.007374    |
| Hydrogen         | 0               | 130.68       | 33.066178    | -11.363417  | 11.432816   | -2.772874    | -0.158558    |
| Carbon           | 716.669         | 158.1        | 21.1751      | -0.812428   | 0.448537    | -0.043256    | -0.013103    |
| H2O              | -241.83         | 188.84       | 30.092       | 6.832514    | 6.793435    | -2.53448     | 0.082139     |
| CO               | -110.53         | 197.66       | 25.56759     | 6.09613     | 4.054656    | -2.671301    | 0.131021     |
| Temperature (oC) | Temperature (K) | T(K)/1000    | H methane    | HO2         | H Carbon    | H H2O        | H CO2        |
| 25               | 298.15          | 0.29815      | -74.87190289 | -0.00027175 | 716.6720711 | -241.8258731 | -393.5253202 |
| 80               | 353.15          | 0.35315      | -72.85059268 | 1.62465731  | 717.8178456 | -239.9706621 | -391.415172  |
| 150              | 423.15          | 0.42315      | -70.06002527 | 3.725236139 | 719.2764554 | -237.578723  | -388.553384  |
| 250              | 523.15          | 0.52315      | -65.58387918 | 6.805980067 | 721.3592218 | -234.0836327 | -384.1761278 |
| 350              | 623.15          | 0.62315      | -60.51781359 | 9.98933393  | 723.4400995 | -230.4819825 | -379.5140465 |
| 425              | 698.15          | 0.69815      | -56.34486143 | 12.43883388 | 724.9994782 | -227.7047492 | -375.859961  |
| 450              | 723.15          | 0.72315      | -54.88589686 | 13.26504578 | 725.5190484 | -226.7639611 | -374.6154071 |
| 475              | 748.15          | 0.74815      | -53.39406668 | 14.09514029 | 726.0385173 | -225.8155193 | -373.358569  |
| 500              | 773.15          | 0.77315      | -51.87007752 | 14.92840565 | 726.5578917 | -224.8593599 | -372.0899952 |
| 525              | 798.15          | 0.79815      | -50.31464956 | 15.76404482 | 727.0771787 | -223.8954282 | -370.81021   |
| 550              | 823.15          | 0.82315      | -48.72851237 | 16.60117544 | 727.5963861 | -222.9236785 | -369.5197146 |
| 575              | 848.15          | 0.84815      | -47.11240153 | 17.43882983 | 728.1155216 | -221.9440731 | -368.2189876 |
| 600              | 873.15          | 0.87315      | -45.46705579 | 18.27595491 | 728.6345934 | -220.9565825 | -366.9084854 |
| 625              | 898.15          | 0.89815      | -43.79321471 | 19.1114122  | 729.1536097 | -219.9611848 | -365.5886429 |
| 650              | 923.15          | 0.92315      | -42.09161669 | 19.94397781 | 729.6725791 | -218.9578657 | -364.259874  |
| 675              | 948.15          | 0.94815      | -40.36299735 | 20.77234238 | 730.19151   | -217.9466179 | -362.9225715 |
| 700              | 973.15          | 0.97315      | -38.60808804 | 21.5951111  | 730.710411  | -216.9274415 | -361.5771079 |
| 725              | 998.15          | 0.99815      | -36.82761474 | 22.41080374 | 731.2292908 | -215.9003434 | -360.2238352 |
| 750              | 1023.15         | 1.02315      | -35.02229699 | 23.21785451 | 731.7481582 | -214.8653372 | -358.8630854 |
| 775              | 1048.15         | 1.04815      | -33.19284703 | 24.01461216 | 732.2670218 | -213.8224435 | -357.4951705 |
| 800              | 1073.15         | 1.07315      | -31.33996904 | 24.7993396  | 732.7858905 | -212.7716893 | -356.1203829 |
| 825              | 1098.15         | 1.09815      | -29.46435853 | 25.57021566 | 733.3047729 | -211.7131082 | -354.7389952 |
| 850              | 1123.15         | 1.12315      | -27.56670171 | 26.32533148 | 733.8236778 | -210.6467404 | -353.3512605 |
| 875              | 1148.15         | 1.14815      | -25.64767508 | 27.06269414 | 734.342614  | -209.5726324 | -351.9574124 |
| 900              | 1173.15         | 1.17315      | -23.70794495 | 27.78022483 | 734.8615899 | -208.490837  | -350.5576653 |
| 925              | 1198.15         | 1.19815      | -21.74816709 | 28.47575923 | 735.3806144 | -207.4014137 | -349.1522142 |
| 950              | 1223.15         | 1.22315      | -19.76898638 | 29.14704747 | 735.899696  | -206.3044277 | -347.741235  |
| 975              | 1248.15         | 1.24815      | -17.77103657 | 29.79175415 | 736.4188432 | -205.1999511 | -346.3248843 |
| 1000             | 1273.15         | 1.27315      | -15.75493999 | 30.40745833 | 736.9380645 | -204.0880616 | -344.9032999 |

F

G

H

|           |            |           |
|-----------|------------|-----------|
| -76.84376 | 158.7163   | -74.8731  |
| -403.6075 | 228.2431   | -393.5224 |
| -8.903471 | 246.7945   | 0         |
| -9.980797 | 172.707974 | 0         |
| 710.347   | 183.8734   | 716.669   |
| -250.881  | 223.3967   | -241.8264 |
| -118.0089 | 227.3665   | -110.5271 |

$$C_p^\circ = A + B*t + C*t^2 + D*t^3 + E/t^2$$

$$H^\circ - H^\circ_{298.15} = A*t + B*t^2/2 + C*t^3/3 + D*t^4/4 - E/t + F - H$$

$$S^\circ = A^* \ln(t) + B*t + C*t^2/2 + D*t^3/3 - E/(2*t^2) + G$$

$C_p$  = heat capacity (J/mol\*K)

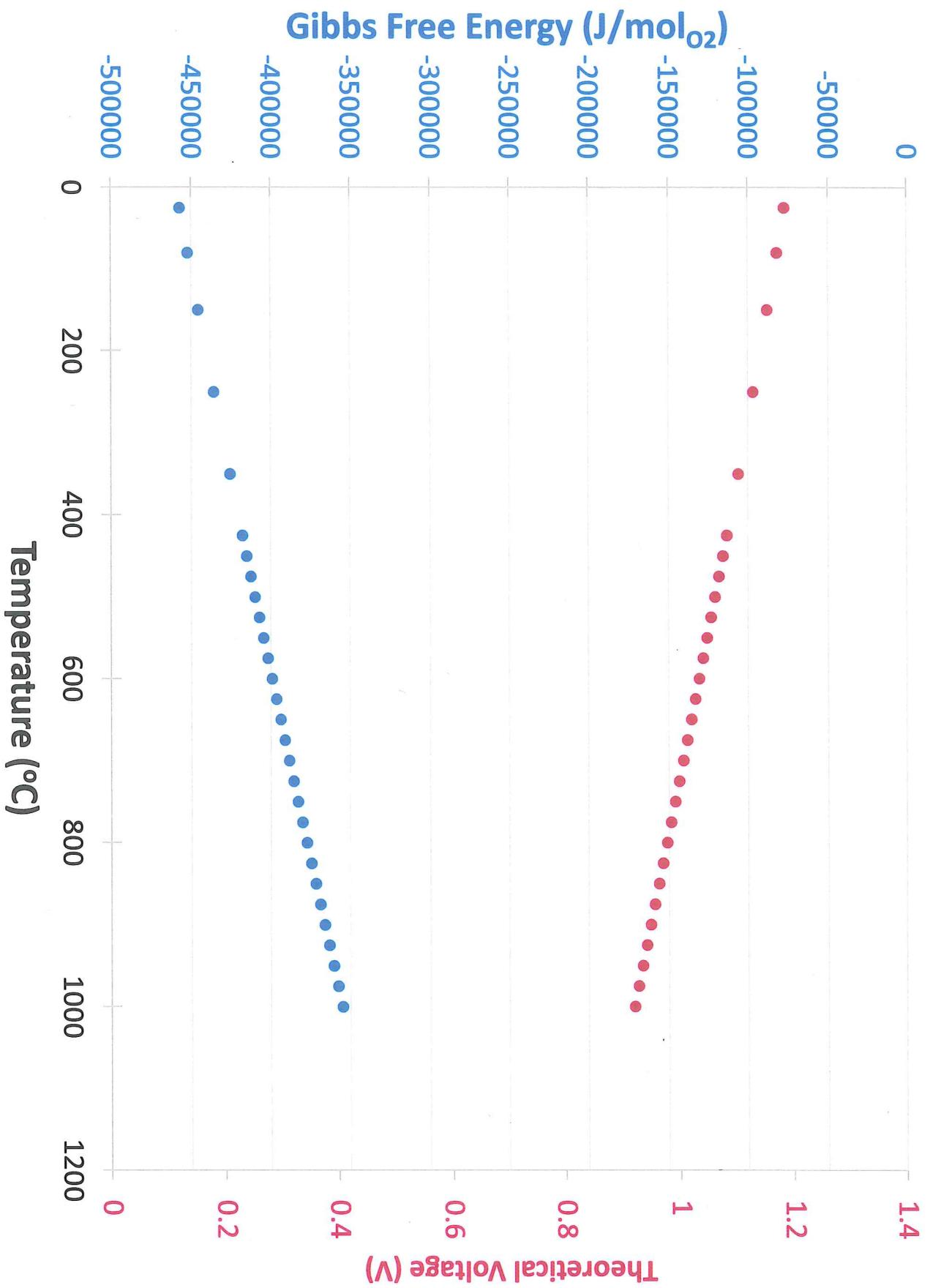
$H^\circ$  = standard enthalpy (kJ/mol)

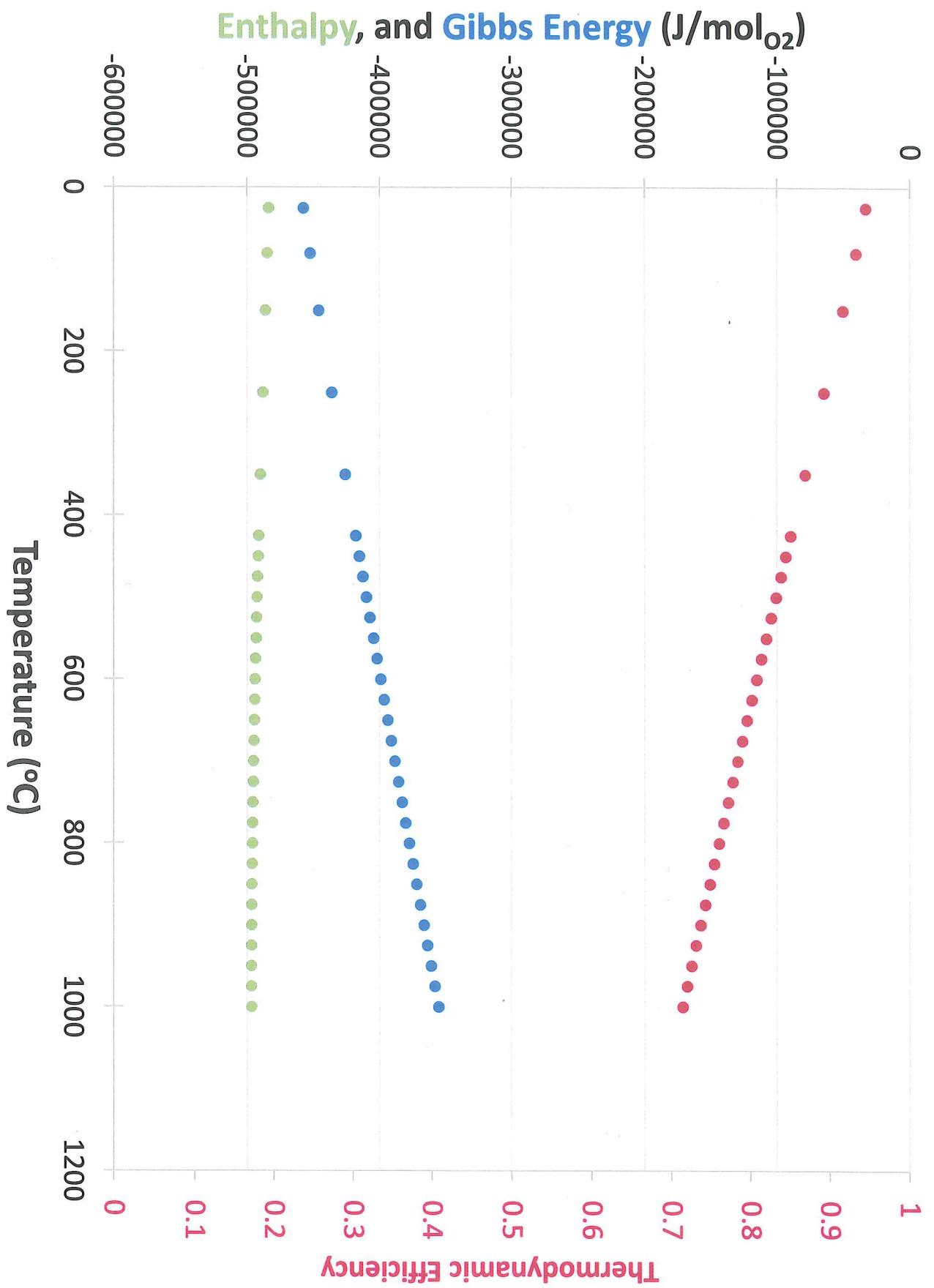
$S^\circ$  = standard entropy (J/mol\*K)

| H CO         | H Hydrogen  | Smethane    | SO2         | S carbon    | SH2O        | SCO2        | SCO         |
|--------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| -110.5238729 | 0.000149248 | 186.2547011 | 205.1472787 | 158.0992005 | 188.8352692 | 213.7876341 | 197.6628841 |
| -108.9214338 | 1.593975211 | 192.4708852 | 210.1481735 | 161.6259924 | 194.5450771 | 220.2771571 | 202.5953443 |
| -106.8728401 | 3.635041449 | 199.6694537 | 215.5730819 | 165.3940837 | 200.7227242 | 227.6630021 | 207.886893  |
| -103.9059583 | 6.559574395 | 209.143036  | 222.1048394 | 169.8125579 | 208.1335244 | 236.9372443 | 214.1787761 |
| -100.8767537 | 9.490177385 | 217.989701  | 227.6705444 | 173.45246   | 214.4306335 | 245.0855104 | 219.4757243 |
| -98.55962807 | 11.69425212 | 224.3084721 | 231.381564  | 175.8153853 | 218.6379846 | 250.6207287 | 222.9862724 |
| -97.77842269 | 12.43064372 | 226.361547  | 232.5442809 | 176.5465809 | 219.9619314 | 252.3721469 | 224.0856504 |
| -96.99279547 | 13.16807305 | 228.3895245 | 233.6727583 | 177.2527852 | 221.2512828 | 254.0807381 | 225.1536723 |
| -96.20276186 | 13.90665525 | 230.3931257 | 234.7683118 | 177.9356503 | 222.5083975 | 255.7485967 | 226.1923796 |
| -95.40834887 | 14.64650533 | 232.3729855 | 235.8320227 | 178.5966712 | 223.7353972 | 257.377648  | 227.203604  |
| -94.60959421 | 15.38773722 | 234.3296683 | 236.8647673 | 179.237205  | 224.9341965 | 258.9696676 | 228.1889946 |
| -93.80654568 | 16.13046296 | 236.2636808 | 237.8672406 | 179.8584871 | 226.106528  | 260.5262992 | 229.1500403 |
| -92.9992606  | 16.87479203 | 238.1754819 | 238.8399781 | 180.4616457 | 227.2539641 | 262.0490683 | 230.088089  |
| -92.18780537 | 17.62083084 | 240.0654904 | 239.7833735 | 181.0477135 | 228.3779354 | 263.5393959 | 231.0043645 |
| -91.37225507 | 18.36868221 | 241.9340922 | 240.697694  | 181.6176383 | 229.4797462 | 264.998609  | 231.89998   |
| -90.55269315 | 19.11844504 | 243.7816451 | 241.5830942 | 182.1722921 | 230.5605887 | 266.4279506 | 232.7759506 |
| -89.72921118 | 19.87021394 | 245.6084833 | 242.4396277 | 182.7124788 | 231.6215544 | 267.8285879 | 233.6332035 |
| -88.90190857 | 20.62407898 | 247.4149212 | 243.2672571 | 183.2389413 | 232.6636449 | 269.2016201 | 234.4725877 |
| -88.07089243 | 21.38012543 | 249.201256  | 244.0658634 | 183.7523671 | 233.6877806 | 270.5480843 | 235.2948812 |
| -87.23627735 | 22.13843358 | 250.9677708 | 244.8352534 | 184.2533943 | 234.6948085 | 271.8689622 | 236.1007988 |
| -86.3981853  | 22.89907852 | 252.7147358 | 245.5751671 | 184.7426157 | 235.68551   | 273.1651844 | 236.8909974 |
| -85.55674547 | 23.66213006 | 254.4424108 | 246.2852838 | 185.2205832 | 236.6606059 | 274.4376353 | 237.6660821 |
| -84.71209418 | 24.42765253 | 256.1510465 | 246.9652272 | 185.6878112 | 237.6207628 | 275.6871573 | 238.4266107 |
| -83.8643748  | 25.1957047  | 257.8408854 | 247.6145706 | 186.1447803 | 238.5665976 | 276.9145543 | 239.1730978 |
| -83.01373762 | 25.96633969 | 259.5121632 | 248.2328414 | 186.5919401 | 239.4986816 | 278.1205947 | 239.906019  |
| -82.16033982 | 26.73960484 | 261.1651095 | 248.8195244 | 187.0297114 | 240.417545  | 279.3060148 | 240.6258138 |
| -81.30434541 | 27.51554169 | 262.7999488 | 249.374066  | 187.4584893 | 241.3236797 | 280.4715209 | 241.3328889 |
| -80.44592514 | 28.29418587 | 264.416909  | 249.8958768 | 187.8786445 | 242.2175427 | 281.6177921 | 242.0276209 |
| -79.58525648 | 29.07556705 | 266.0161816 | 250.3843346 | 188.2905258 | 243.0995589 | 282.7454822 | 242.7103586 |

Fuel Cell: 2H2+O2 -> 2H2O

| S Hydrogen  | Delt H (J/mol) | delt S (J/mol K) | delt G (J/mol) | Vcell       | efficiency  |
|-------------|----------------|------------------|----------------|-------------|-------------|
| 130.6801501 | -483651.7729   | -88.83704046     | -457165.0093   | 1.184545753 | 0.94523588  |
| 135.5855369 | -484753.932    | -92.22909329     | -452183.2277   | 1.171637617 | 0.932809819 |
| 140.8579734 | -486152.765    | -95.84358045     | -445596.5539   | 1.154571095 | 0.916577228 |
| 147.0618868 | -488092.3942   | -99.96156421     | -435797.5018   | 1.129181082 | 0.892858621 |
| 152.1878902 | -489933.6537   | -103.1850578     | -425633.885    | 1.102846457 | 0.868758212 |
| 155.5276039 | -491236.8366   | -105.1608026     | -417818.8223   | 1.082597096 | 0.850544567 |
| 156.5639293 | -491654.2555   | -105.7482767     | -415182.3892   | 1.075765918 | 0.844460074 |
| 157.5664403 | -492062.325    | -106.3030733     | -412531.6807   | 1.068897751 | 0.833837283 |
| 158.5375116 | -492460.4359   | -106.8265399     | -409867.4965   | 1.061994668 | 0.832285127 |
| 159.479291  | -492847.9119   | -107.3198104     | -407190.6053   | 1.05505866  | 0.826199311 |
| 160.3937263 | -493224.0069   | -107.7838269     | -404501.7497   | 1.048091652 | 0.820117724 |
| 161.282588  | -493587.902    | -108.2193606     | -401801.6513   | 1.041095512 | 0.814042746 |
| 162.1474894 | -493938.704    | -108.6270287     | -399091.0139   | 1.034072066 | 0.807976801 |
| 162.9899037 | -494275.4436   | -109.0073101     | -396370.528    | 1.027023101 | 0.801922356 |
| 163.8111787 | -494597.0736   | -109.360559      | -393640.8736   | 1.01995038  | 0.79588193  |
| 164.61255   | -494902.4684   | -109.6870169     | -390902.7233   | 1.012855646 | 0.7898581   |
| 165.3951523 | -495190.4221   | -109.9868235     | -388156.7448   | 1.005740628 | 0.783853499 |
| 166.1600292 | -495459.6485   | -110.2600257     | -385403.6038   | 0.998607052 | 0.777870822 |
| 166.9081423 | -495708.7798   | -110.5065868     | -382643.9655   | 0.99145664  | 0.771912827 |
| 167.6403784 | -495936.3663   | -110.7263931     | -379878.4974   | 0.984291124 | 0.765982338 |
| 168.357557  | -496140.8755   | -110.9192612     | -377107.8704   | 0.97711224  | 0.760082245 |
| 169.060436  | -496320.6922   | -111.084944      | -374332.7609   | 0.969921742 | 0.754215504 |
| 169.7497171 | -496474.1173   | -111.2231359     | -371553.8522   | 0.9627214   | 0.748385141 |
| 170.426051  | -496599.3682   | -111.3334774     | -368771.8361   | 0.955513006 | 0.742594251 |
| 171.0900411 | -496694.5783   | -111.4155602     | -365987.4138   | 0.948298378 | 0.736846001 |
| 171.742248  | -496757.7962   | -111.4689303     | -363201.2974   | 0.94107936  | 0.731143628 |
| 172.3831928 | -496786.9863   | -111.4930921     | -360414.2107   | 0.933857828 | 0.725490443 |
| 173.01336   | -496780.028    | -111.4875114     | -357626.8906   | 0.926635691 | 0.719889831 |
| 173.6332007 | -496734.7157   | -111.4516184     | -354840.0877   | 0.919414895 | 0.714345256 |





What if our reaction is not @ STP?



$$\Delta G = \Delta G^\circ + RT \ln \left( \frac{q_R^{V_R}}{q_0^{V_0}} \right)$$

$$-nFE_{eq} = -nFE^\circ + RT \ln \left( \frac{q_R^{V_R}}{q_0^{V_0}} \right)$$

$$E_{eq} = E^\circ - \frac{RT}{nF} \ln \left( \frac{q_R^{V_R}}{q_0^{V_0}} \right)$$

$$\boxed{E_{eq} = E^\circ + \frac{RT}{nF} \ln \left( \frac{q_0^{V_0}}{q_R^{V_R}} \right)} \Rightarrow \text{Nernst Equation}$$

$$\text{for liquid: } q_i = \gamma_i C_i$$

$$\text{for vapor: } q_i = \gamma_i P_i$$

$$\text{for solid } q_i \approx 1$$

For liquids:

$$E_{eq} = E^{\circ} + \frac{RT}{nF} \ln \left( \frac{\gamma_0^{V_0} C_0^{V_0}}{\gamma_2^{V_2} C_2^{V_2}} \right)$$

$$E_{eq} = E^{\circ} + \frac{RT}{nF} \ln \left( \frac{\gamma_0^{V_0}}{\gamma_2^{V_2}} \right) + \frac{RT}{nF} \ln \left( \frac{C_0^{V_0}}{C_2^{V_2}} \right)$$

$E^{oi}$  ≡ Formal Potential

$$E^{oi} = E^{\circ} + \frac{RT}{nF} \ln \left( \frac{\gamma_0^{V_0}}{\gamma_2^{V_2}} \right)$$

When  $\gamma_0 = \gamma_2 = 1$ :

$E^{oi} = E^{\circ} \Rightarrow$  Common Assumption!

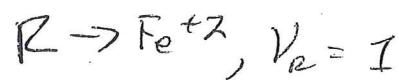
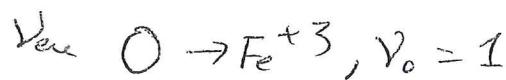
$$E_{eq} = E^{oi} + \frac{RT}{nF} \ln \left( \frac{C_0^{V_0}}{C_2^{V_2}} \right)$$

Most Common  
Form of the Nernst Eqn!

→ relate to Al/air cell     $[O_2] \sim 2 \times 10^{-4} M$   
 $[Al^{(eth)}] \sim$  very low (initially no!)

(9)

Example :



•

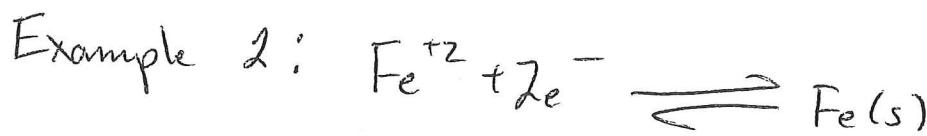
$$E_{\text{eq}} = E^{\circ} + \frac{RT}{nF} \ln \frac{[Fe^{+3}]}{[Fe^{+2}]}$$

if we assume:  $\gamma_o = \gamma_r \approx 1$

$$E^{\circ} \approx E^o$$

$$E_{\text{eq}} = E^o + \frac{RT}{nF} \ln \frac{[Fe^{+3}]}{[Fe^{+2}]}$$

$$E_{\text{eq}} = 0.77 V + \frac{RT}{nF} \ln \frac{[Fe^{+3}]}{[Fe^{+2}]}$$



Assume  $\gamma'_s = 1$

$$E_{\text{eq}} = \cancel{Q} E^o + \frac{RT}{nF} \ln \left( \frac{Q_{Fe^{+2}}}{Q_{Fe}} \right)$$

$$E_{\text{eq}} = E^o + \frac{RT}{nF} \ln Q_{Fe^{+2}} = E^o + \frac{RT}{nF} \ln (\gamma_{Fe^{+2}} C_{Fe^{+2}})$$

$$E_{\text{eq}} = E^o + \frac{RT}{nF} \ln [Fe^{+2}]$$

$$E_{\text{eq}} = -0.44 + \frac{RT}{nF} \ln [Fe^{+2}]$$

(10)